

Design and Analysis of Algorithms  
PhD Coursework, Semester-II, Session: 2023-24  
**Assignment-I**

Maximum Marks  $\in \{5, 6, \dots, 10\}$

Submission Deadline: **2023-Mar-10**

**Comparing Sorting Algorithms**

1. Consider all sorting algorithms taught in the classes. For example, Bubble Sort, Selection Sort, Insertion Sort, Merge Sort, Quick Sort, Heap Sort, Counting Sort, and Radix Sort.
2. **Time Complexity Analysis:**
  - a. Best-case: Identify the scenario where the algorithm performs the fastest and analyze its time complexity in terms of Big O notation (e.g.,  $O(n)$ ).
  - b. Average-case: Analyze the expected time complexity for a randomly ordered input. Most efficient algorithms have an average-case complexity of  $O(n \log n)$ .
  - c. Worst-case: Determine the scenario leading to the slowest performance and analyze its time complexity (e.g.,  $O(n^2)$ ).
3. **Space Complexity Analysis:**
  - a. Analyze the additional memory space required by each algorithm during the sorting process. This could be constant ( $O(1)$ ) for in-place algorithms or linear ( $O(n)$ ) for algorithms using extra data structures.
4. **Additional Considerations:**
  - a. Stability: Discuss whether the algorithm preserves the original order of elements with equal values.
  - b. Adaptability: Analyze if the algorithm performs better when the input is partially sorted or has limited unique values.
  - c. Parallelizability: Discuss the potential for implementing the algorithm on multiple processors to improve performance.
5. **Deliverables:**
  - a. Report: Summarize your findings in a **comparison table**, in Latex2e.
  - b. Individual Algorithm Analysis: For each algorithm, dedicate a section analyzing:
    - i. Time complexity (best, average, worst case)
    - ii. Space complexity
    - iii. Stability, adaptability, and parallelizability considerations
  - c. Conclusion: Summarize the key differences between the analyzed algorithms, highlighting their strengths and weaknesses in different scenarios.
  - d. References (Mandatory): Include references to any resources used during your research.

6. **Submission:** Send the latex code to the submission portal together with pdf in a zip file (filename format `assign1_firstname.zip`)
7. **Collaboration:** Collaboration is allowed with at most two friends. In such cases, each collaborator will receive at most 75% of the marks obtained. The contribution of each collaborator, in percentage, should be specified in the submitted document.  
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